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Production Data Analysis Techniques for the Evaluation of the Estimated Ultimate Recovery (EUR) in Oil and Gas Reservoirs

Saber Kh. Elmabrouk ¹, Walid Mohamed Mahmud ^{2*}[®]

¹ Chemical & Petroleum Engineering, School of Engineering and Applied Science, The Libyan Academy, Tripoli, Libya.
² Department of Petroleum Engineering, Faculty of Engineering, University of Tripoli, Tripoli, Libya.

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Abstract

The calculation of oil reserves (estimate ultimate recovery, EUR) is required for reservoir management. It is important to differentiate between oil reserves and oil resources. The latter is roughly defined as the sum of recoverable and unrecoverable volumes of oil in place; whereas, the oil reserves can be defined as those amounts of oil anticipated to be commercially recoverable from a given date under defined conditions. However, there is always uncertainty when making reserve estimates, and the main source of uncertainty is the lack of available geological data. Depending on the quantity and quality of the available data, different methods are used for the evaluation of the EUR. A number of essentially straight-line extrapolation techniques (production data analysis) have been proposed to estimate the EUR for oil and gas wells. Thus, a detailed analysis of past performance of oil and water production data is required in order to predict the future performance of the oil and gas wells. This work utilized seven straight-line extrapolation techniques to estimate and compare the values of EUR of three oil wells from the same reservoir. The comparison shows very similar estimated EUR.

Keywords: Estimated Ultimate Recovery; Water Oil Ratio; Reserve; X-plot; Production Data Analysis; Decline Curve Analysis.

1. Introduction

The calculation of expected initial oil in place and estimated ultimate recovery (EUR) of oil and gas wells are required for evaluation and reservoir management purposes. It is important to differentiate between oil reserves (EUR) and initial oil in place. The latter is roughly defined as the sum of recoverable and unrecoverable volumes of oil in place. Whereas, the oil reserves can be defined as those amounts of oil anticipated to be commercially recoverable by applying development projects to known accumulations from a given date under defined conditions. However, there is always uncertainty when making reserve estimates. The main source of uncertainty is the lack of available geological data. Depending on the quantity and quality of the available data, different methods are used for the evaluation of the EUR [1-3]. For example, in the initial stage of development of the hydrocarbon deposit, there is very little information available; therefore, approximate estimates are usually made using analog or volumetric calculations. Considering that, in the late stage of reservoir development, production data analysis and reservoir simulation methods are commonly employed. However, it is worthwhile to mention that the EUR is the most important step toward taking any decisions regarding drilling activities, field development and reservoir management. Simultaneously, it is the most difficult aspect of reservoir engineering, especially in the early life of the reservoir. Several methods are used to

* Corresponding author: w.mahmud@uot.edu.ly

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estimate an EUR, and the methods differ depending upon the purpose of the study and availability of the data. Mainly, there are six methods available in the literature to estimate the oil and gas reserves; Volumetric Method [4], Material Balance Method [5], Production Decline Analysis (DCA) [6], Type Curve Analysis (TCA) [7], Numerical Simulation Method [8], Water Oil Ratio (WOR) [9] data analysis.

Commonly, oil and water production data are regularly measured with time. Most oil wells which are produced by natural water drive or a pressure maintenance waterflood will produce water along with oil during their life. Oil and water production history can be used in a number of ways; however, the DCA, and WOR data analysis techniques are utilized in this study where the historical oil and water production data for three selected oil wells was analyzed in order to determine EUR. In most cases, WOR is used as an analytical tool. WOR data is a performance-based method of trending future water production for the purpose of forecasting oil production, water production, and determining expected EUR. Water-cut (WC) or water fractional flow (f_w) and oil-cut or oil fractional flow (f_o) are alternatives ratio forecasting methods to WOR. All the proposed techniques consider straight-line relationship techniques and extrapolating the past performance on the plot.

A number of essentially empirical methods have been proposed in the literature to evaluate the waterflood performance and to calculate the EUR that consider the linearity of late-time behavior of the WOR. The objective of those efforts was to provide a semi-analytical representation for natural water drive and/or waterflooding mechanisms in oil production. Nevertheless, the oil production decline is caused by reduction in oil saturation and oil relative permeability. Unfortunately, in most cases, this method is applicable only for the analysis of late stage of a waterflood (for values of WC greater than 50%). The expression for the steady-state radial flow of oil and water are presented in Equation 1. Simultaneously, f_w in the reservoir is the ratio of the water production rate and the total liquid production as illustrated in Equations 2 and 3. Likewise, oil fractional flow, f_o , is the ratio of the oil production to the total liquid production.

$$q = \frac{kh}{141.2 B\mu} \frac{1}{l \operatorname{n}\left(\frac{r_e}{r_W}\right)} \Delta p \tag{1}$$

$$f_w = \frac{q_w}{q_w + q_o} \tag{2}$$

From 1 and 2 we get:

$$f_w = \frac{1}{1 + \frac{k_o \mu_w B_w}{k_w \mu_o B_o}} \tag{3}$$

$$f_o = \frac{q_o}{q_w + q_o} \tag{4}$$

Since all the used techniques to establish the EUR mentioned are depending on a straight-line trend, Espinel and Barrufet (2009) [10] wondered about the accuracy of the selection of the straight-line zone. Is the straight-line zone always present? How long is it? Is it always correct to extrapolate it to find ultimate recovery at an assumed economic limit? Where does the straight-line zone begin and where does it end? They developed an alternative technique, based on multiple regression analysis, to calculate reservoir performance and EUR. The proposed method provides slops and intercepts of straight line zone of the plot of the WOR versus recovery factors from the water breakthrough time to the point where the maximum economic recovery factor.

Generally speaking, the lifecycle of an oilfield is typically characterized by three main stages: production build-up, plateau production, and declining production. Sustaining the levels of production required during the duration of the life cycle requires a good understanding and the ability to control the recovery mechanisms involved. One of the more significant key elements that effecting oil production rates during the life cycle of the field is downhole environment. It was confirmed by Ben Mahmud et al. (2016) [11] and Busahmin et al. (2017) [12] that when production wells were drilled and completion properly, they show a significant impact on the oil recovery.

2. Oilfield Case Studies

A detailed analysis of the past oil, gas and water production performance was conducted for the simultaneous evaluation of EUR. However, due to the uncertainty in the accuracy of extrapolation methods, as well as the lack of a completely rigorous mathematical basis, this study applies seven different extrapolation techniques:

- Decline curve analysis
 - \circ Log(q_o) versus production time, t;
 - $\circ q_o$ versus N_p ;
 - $\circ 1/q_o$ versus t_o ;

- WOR extrapolated methods
 - \circ Log(f_w) versus N_p ;
 - $\circ f_o$ versus N_p ;
 - $\circ 1/f_w$ versus N_p , and;
- X-plot technique
 - $\circ N_p$ versus X-function.

Such an approach would provide a validation for the EUR results, and although there is no single perfect extrapolation technique, comparing the results obtained from different methods would provide consistency and a validation element. In this case study, three oil wells (A-01, A-06 and A-28) from a Libyan oilfield located in Sirte Basin (Figure 1) were selected to utilize seven straight-line extrapolation techniques to estimate and compare the values of EUR.



Figure 1. The Sirte Basin is a Libyan oilfield [13]

(9)

2.1. Decline Curve Analysis (DCA)

Arps (1945) [14] proposed the curvature in the production rare versus time. The method can be described by doing a plot of oil or gas production data rate versus time that could be extrapolated to provide an estimate of future rate of production for a well or a field. With this forecasting, it is possible to determine the EUR of the well or the field. However, the basic assumption in the DCA is that the parameters controlling the decline trend of the curve in the past will continue to govern the trend in the future in a uniform manner. However, the normal shape of the decline curve effected by several factors: (1) Human factors, such as restricted production rate to the allowable rate setup by regulatory body, marketing, or due to shutting down of wells for well testing, workover, etc. (2) Production conditions, such as changing the number of producers, changing the lift conditions, changing the productivity index due to permeability changing around the wellbore, and changing the surface conditions. (3) Reservoir factors, such as reservoir drive mechanism, reservoir rock and fluid properties, relative permeability curves and using of water injection, water flooding and EOR techniques.

DCA uses empirical equations that models how the flow rate changes with time assuming a certain decline rate. It is one of the most used forms of data analysis to evaluate gas and oil reserves and predict future production. This technique is based on the assumption that past production trends and their control factors will continue in the future and; therefore, can be extrapolated and described by one of the three mathematical expressions; (1) Exponential decline (2) Harmonic decline and (3) Hyperbolic decline. A major assumption here is that the most dominant past behavior will govern the future behavior of the well's performance. Obviously, this is not necessarily true but works in many cases. It could also yield reasonable results when more wells are lumped together. However, this technique ignores any geological information from the field and, therefore, could give very unreasonable results in some cases.

There are some factors that affect the trend of production decline. the main factors may include; (1) Human factors (such as the restriction of the production rate to the allowable rate setup by the regulatory body, restriction due to the marketing or shutting down of wells for well testing), (2) production conditions (such as changing number of producers, changing lifting conditions, changing the productivity index of the well due to acidification, damage, hydraulic fracturing or re-perforations), or Change surface conditions (such as changing the well head pressure or separator pressure), and (3) reservoir factors (such as reservoir drive mechanisms, reservoir fluid and rock properties or the use of pressure maintenance, waterflooding and EOR techniques). Equation 5 presents the general form for decline curve analysis, and Equation 6 presents the cumulative production formula. However, exponential (b=0) and harmonic (b=1) decline are special cases of these formulas.

$$q = \frac{q_i}{(1+D \ b \ t)^{1/b}}$$
(5)
$$N_p = \frac{q_t^b}{D^{(1-b)}} \left[q_i^{1-b} - q^{1-b} \right]$$
(6)

Variables;

q =Current production rate;

 q_i = Initial production rate (start of production);

D = Initial nominal decline rate at t = 0;

t = Cumulative time since start of production;

b = Decline constant normally has a value 0 < b < 1;

 N_p = Cumulative production being analyzed.

The exponential decline curve technique uses a semi log plot of q versus t. In general, this plot provides a linear trend, which can be extrapolated to any future time or a desired economic production limit. The corresponding value of Np can be estimated from that extrapolation. The governing equation for the case of the exponential production decline is given by Equation 7.

$$q_o = q_i e^{-Dt} \tag{7}$$

From Equation 7, a rate-cumulative production relationship can be developed. The definition of cumulative production is given by:

$$Np = \int_0^t q_o dt \tag{8}$$

Substituting Equation 7 into Equation 8 and integrating yields:

$$Np = \int_0^{\tau} q_i e^{-Dt} dt = \frac{1}{D} \{ q_i - q_i e^{-Dt} \}$$

Substituting Equation 8 into the last part of Equation 9 yields:

$$Np = \frac{1}{D}(q_i - q_o) \tag{10}$$

Equation 10 can be used to obtain the EUR by using the data obtained from the plot of q_o versus t and at a desired economic production limit. In addition, by solving Equation 10 for q_o the rate-cumulative production relationship can be obtained as in Equation 10.

$$q_o = q_i - DNp \tag{11}$$

$Log(q_o)$ versus Production Time, t

The three oil wells were found to be declining exponentially (b = 0), and their rate time performances are presented in Figures 2 to 4. Most of the plots presented a linear trend, and the value of the EUR is obtained at q_o value of 100 bpd. The results are summarized in Table 1.



Figure 2. Oil production rate versus production time for well A01



Figure 3. Oil production rate versus production time for well A06

$Log(q_o)$ versus Production Time, t



Table 1. EUR from $log(q_0)$ vs. production time, t

Figure 4. Oil production rate versus production time for well A28

Oil Production Rate, q_o versus Cumulative Oil Production, N_p

The plots of q_o vs N_p for A01, A06 and A28 are presented in the Figures 5 to 7 respectively. The values of the EUR for each well are evaluated at q_o value of 100 bpd. Table 2 illustrated the results of EUR of the wells.



Figure 5. Oil production rate versus cumulative oil production for well A01



Figure 6. Oil production rate versus cumulative oil production for well A06



Figure 7. Oil production rate versus cumulative oil production for well A28

Reciprocal of oil rate, $1/q_o$ versus oil material balance time, t_o

Bondar and Blasingame (2002) [15] and Blasingame and Reese (2007) [16] applied a reciprocal rate method to estimate EUR. The approach required a plot of the reciprocal flowrate (1/q) and material balance time, t_o , (N_p/q) assuming a constant flowing bottom-hole pressure (p_{wf}) , which has the following relation:

$$\frac{1}{q} = c + m \left[\frac{N_p}{q} \right] \tag{12}$$

In contrast, the plot 1/q versus t_o yields a straight line with slop of m = 1/EUR. Nonetheless, Blasingame and Reese (2007) [16] shown that the method should tolerate arbitrary changes in p_{wf} particularly smooth changes. They, also, noticed that this approach has proven to be robust and consistent, likewise, it can be applied in all cases for oil and gas wells and it is more rigorous than Arps approch. Figures 8 to 10 illustrated the reciprocal of oil rate. The plots yield a linear trend for all the time period.



Figure 8. Reciprocal of oil rate, $1/q_o$ versus oil material balance time, to for well A01



Figure 9. Reciprocal of oil rate, $1/q_o$ versus oil material balance time, to for well A06



Figure 10. Reciprocal of oil rate, $1/q_o$ versus oil material balance time, to for well A28

	Tabl	le 3	. 1	EUR	from	reciprocal	l of	oil	rate	versus	oil	material	balance	time
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Well	Straight-line Eq.	EUR
A01	$1/q_o = 1.55\text{E-}05 + 1.91\text{E-}08 t_o$	52.36MM STB
A06	$1/q_o = 7.37\text{E-}05 + 1.56\text{E-}8 t_o$	64.10MM STB
A28	$1/q_o = 2.08 \text{E-}04 + 8 \text{E-}08 t_o$	12.50MM STB

2.2. Semi-steady State WOR Extrapolated Method

The analysis and interpretation of the oil and water production data (WOR, f_w , and f_o functions) take into consideration presence of both the oil and water phases flowing simultaneously in the reservoir. In 1990, Lo et al. [17] suggested using log(WOR) versus N_p to obtain the EUR. They, also, investigated the dependence of the WOR versus N_p plot on different well and reservoir characteristics. The results establish that the slop of the straight-line trend effected by conducting numerical simulations in 2D and 3D systems and by investigation various effects. They concluded that a linear relationship between the log(WOR) and N_p adequately fit many of their results. However, it is important to bear in mind that this type of plot (log WOR versus N_p) cannot be used to directly estimate the value of the EUR as needs some core data.

Chan (1995) [18] used numerical simulation to examine the sensitivity of WOR versus time on various of reservoir and production factors. He conjectured that a log-log plot of the curve can be used to diagnose the origin of the water production. Motivated by Chan's work, Yorsos et al. in 1999 provided a fundamental investigated by conducting analytical and numerical studies of waterflooding under variety of condition to analyze the behavior of WOR curves in various time domains. They concluded that the relationship between the WOR and time contains two effects, one due to the relative permeability and mobility and the other due to the production geometry.

Bondar and Blasingame (2002) [15] discussed various straight-line methods for the WOR functions in various forms (log WOR, log f_w , and f_o) versus the N_p . They, also, proposed two straight-line trend plots to estimate the EUR; $1/f_w$ versus N_p , and $1/q_o$ versus N_p/q_o . The plot of $1/f_w$ versus N_p yields an apparent linear trend that can be extrapolated to provide an estimate of EUR.

To reduce the uncertainty of EUR three analysis plots are applied here for WOR extrapolated method; (1) $Log(f_w)$ versus Np (2) f_o versus N_p , and (3) $1/f_w$ versus N_p . All the plots, however, show a linear trend at late-time WOR behavior when the value of f_w function approaches 0.5 (WC = 50%) or higher. Consequently, the plots can estimate the value of the mobile oil (EUR) by extrapolating the WOR linear trend to an economic limit of the WOR function, which in this study was selected to be at 99% WC. Typically, the plots show a high degree of scatter in the earliest production data, which could be due to the realization that these data represent transient or transition flow behavior.

$Log(f_w)$ Versus N_p

Figures 11 to 13 show the plot of $Log(f_w)$ versus N_p . Obviously, the semi-steady State WOR period produced a straight-line which extrapolated to WC 99% as an economic limit. The results are summarized in Table 4.



Figure 11. Fractional flow of water versus cumulative oil production for well A01



Figure 12. Fractional flow of water versus cumulative oil production for well A06



Figure 13. Fractional flow of water versus cumulative oil production for well A28

Table 4.	EUR	from	$Log(f_w)$) versus	Np
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Well	Straight-line Eq.	EUR
A01	$f_w = 1.87\text{E-07} \exp(2.94\text{E-07} N_p)$	52.67MM STB
A06	$f_{\rm w} = 0.01 \exp(7.16\text{E}-08 N_p)$	64.32MM STB
A28	$f_w = 0.122 \exp(16.9\text{E}-08 N_p)$	12.40MM STB

f_o Versus N_p

Figures 14 to 16 show the plot of f_o versus N_p . The late datapoints (semi-steady state) formed a straight-line trend. This straight line was extrapolated to an economic limit of 99% WC in order to obtain the EUR and summarized in Table 5.

Table 5. EUR from f_o versus N_p

Well	Straight-line Eq.	EUR
A01	$f_o = 12 - 2.28522 \text{E-}07 N_p$	52.51MM STB
A06	$f_o = 8.5 - 1.3381 \text{E-}07 N_p$	63.52MM STB
A28	$f_o = 1.20 - 9.35 \text{E-}08 N_p$	12.80MM STB



Figure 14. Fractional flow of oil versus cumulative oil production for well A01



Figure 15. Fractional flow of oil versus cumulative oil production for well A06



Figure 16. Fractional flow of oil versus cumulative oil production for well A28

$1/f_w$ Versus N_p

The Figures 17 to 19 show the semi-state state of f_w vs N_p extraplotated technique of the well A01, A06 and A28 respectively. The Figures show linear trend of the late datapoints and the results EUR are tabolated in Table 6.



Figure 17. Reciprocal of fractional flow of water versus cumulative oil production for well A01



Figure 18. Reciprocal of fractional flow of water versus cumulative oil production for well A06



Figure 19. Reciprocal of fractional flow of water versus cumulative oil production for well A28

Well	Straight-line Eq.	EUR
A01	$1/f_w = 19 - 3.416 \text{E-} 07 N_p$	52.67MM STB
A06	$1/f_w = 2.62 - 2.5E-08 N_p$	64.80MM STB
A28	$1/f_w = 1.92 - 7.187 \text{E-}08 N_p$	12.80MM STB

Table 6. EUR from $1/f_w$ versus N_p

2.3. X-plot

The X-plot technique is based on fractional flow and the Buckley-Leverett calculations. Based on Ershaghi & Omorigie (1978). [19], an interesting application of the X-plot method is that the linear plot of N_p versus X-function (Equation 12) gives a straight line that can be extrapolated to any desired WC (economic f_w) as a mechanism for determining the corresponding EUR. The extrapolation of the past performance on the plot is a complicated task. The difficulty arises mainly because a curve fitting by simple polynomial approximation does not result in satisfactory answers in most cases. Due to the fact that X-function has a parabolic shape the recommendation is to restrict this technique to f_w greater than 50%. Differentiating X-function with respect to f_w and equating the first derivative to zero can prove this restriction. Ershaghi and Abdassah (1984) [20] provides a detailed explanation of this concept.

$$x = \ln\left(\frac{1}{f_{w}} - 1\right) - \frac{1}{f_{w}}$$
(12)

Lijek (1989) [21] examined various WOR analysis techniques and presented analytical methods by which the oil rate can be modeled as a function of time. He examined the linearity of; WOR versus N_p , X-plot method, and $\frac{1}{WOR}$ + WOR versus cumulative water injection (W_i).

Bondar and Blasingame (2002) [15] considered that the X-plot technique gave the least consistent results compared to the other methods used. straight-line extrapolation methods produced more consistent estimates of EUR than the Xplot technique. Also, they concluded that the X-function plot typically does not develop a clear straight-line trend. According, the logarithm of WOR, WC, or f_w function plotted against N_p is commonly used for evaluation and prediction of waterflood performance. This presumed semi-log plot of f_w and oil recovery allows extrapolation of the straight line to any desired f_w as a mechanism for determining the corresponding EUR. Straight line extrapolation method assumes that the mobility ratio is equal to unity and the plot of the log of relative permeability ratio of the lowing liquids, (k_{rw}/k_{ro}), versus water saturation, s_w , is a straight line.

Yang (2009) [22] proposed two types of linear plots based on so-called *Y*-function (Equation 13 and 14); (1) plotting *Y* versus t_D on the log-log scale gives a straight line trend with a slop of -1 and an intercept of E_V/B , and (2) plotting *Y* versus reciprocal-of-time ($1/t_D$) is also a straight line with an intercipt of zero and a slop of E_V/B .

$$Y = \left(\frac{E_V}{B}\right) \frac{1}{t_D} \tag{13}$$

With the oil-fraction flow, *Y* is defined as;

$$Y = f_0 (1 - f_0)$$
(14)

where *B* is the relative permeability ratio parameter, and E_v is the volumetric sweep efficincy. The parameter t_D is the ratio of cumulative liquid production to the total pore volume (*PV*) of the waterflood pattern area (swept and unswept). Yang indicated that forecasting can be performed with the historical-production data without needing to calculate parameter E_v and *B* or without the need of knowing reservir volume. Plotting *Y* vesus Q_L and *Y* versus $1/Q_L$ on log-log scale yaldeis the features. Likewise, he showed that these plots can be applied to forecast the oil fraction flow and then to calculate the oil rate with known liquid rate. The analysis technique improve the reliability of EUR and production forecasts. The *Y*-function method, as a performance diagnostic analysis method, can diagnose the production history for breakthrough timing. The flow regime diagram of the *Y*-function versus cumulative liquid production on the log-log scale are presented in Figure 20. A nearly constant *Y*-function starts to decline with slop of -1 (Yang, 2012) [23].

In a more recent study, Yang (2017) [24] declared that the waterflood analytical methods are obtained by solving 1D Buckly-Levertt equations [25] in the X-plot conditions. The dependent variable can be classified into two groups: cumulative production (oil, water, liquid or recovery factor) and water-cut feature variables. The water-cut feature variables can be various forms: f_w , f_o , WOR, X-plot function or Y-function. As well, he proposed analytical approach for X-plot method as follows: (1) use Y-function to confirm water breakthrough timing, to clarify possible impact or

reconfiguration events, and to select a post-breakthrough reference point on the linear trend; (2) obtain cumulative liquid and oil (Q_L , Q_o) and f_o for the reference point; and (3) calculate the slop, m of the straight-line trend and the X-value on the reference point, which will then solve for the intercept, n. When the parameters m and n are available, the X-plot method is used to predict the EUR. He concluded that the procedure of combining the X-plot method and Y-function method will reduce uncertainty in the EUR determination.

$$X = ln\left(\frac{1}{f_{w}} - 1\right) - \frac{1}{f_{w}}; \ n = \left(S_{w} - \frac{1}{B}ln\frac{A}{M}\right); \ m = \frac{1}{B}$$
(15)

Where *M* is the mobility ratio, *B* is a constant in the expression of the straight line in the semi-log oil to water relative permeability versus water saturation $(k_{ro}/k_{rw} = Ae^{-BS_w})$, and *A* is a constant.



Figure 20. Flow-regime diagram for production surveillance

Bondar and Blasingame (2002) [15] mentioned that in all of the cases they considered, the X-plot technique gave the least consistent results compared to the other methods used. Contrary, Yang (2017) [24] reported that applying of X-plot method in analytical approach reduces uncertainty in the EUR determination. In this study the X-plot of the three oil wells show that the late datapoints formed a straight-line trend as described in Figures 21 to 23. The assessment of EUR are illustrated in Table 7.



Figure 21. X-plot for well A01



Figure 22. X-plot for well A06



Figure 23. X-plot for well A28

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Well	Straight-line Eq.	EUR
A01	$N_p = 5.2E + 07 - 51000 X$	52.40MM STB
A06	$N_p = 5.8E+07 - 9.8E+05 X$	64.00MM STB
A28	Np = 10900000-250000 X	12.30MM STB

3. Conclusions

Estimated ultimate recovery of oil and gas wells are required for evaluation and reservoir management purposes even though there is always uncertainty when making reserve estimates. Depending on the quantity and quality of the available data, different methods are used for the evaluation of the EUR. Employment of oil and water production data for reserve estimate have a certain degree of uncertainty; therefore, different methods should be applied to reduce this uncertainty. In fact, oil and water production data are regularly measured with time, which can be analyzed in a number of ways. The analysis and interpretation of the oil and water production data (WOR, f_w , and f_o functions) take into consideration presence of both the oil and water phases flowing simultaneously in the reservoir. In particular, this paper provides verification and application of calculating the EUR from oil and water production data. The analysis consisted of performing plots of different OWR functions versus time or cumulative production that could be extrapolated to provide an estimate of future rate of production for a well or a field. The success of this method depends on our selection of straight line points. Three field examples from Libyan oilfield were analyzed with seven different extrapolation techniques:

- $log(q_o)$ versus production time, *t*;
- q_o versus N_p ;
- $1/q_o$ versus t_o
- $log(f_w)$ versus N_p ;
- *f_o* versus *N_p*;
- $1/f_w$ versus N_p , and;
- N_p versus X-function.

These techniques should be applied simultaneously in order to obtain consistent approximate of the EUR. We believe that due to the uncertainty in the accuracy of these extrapolation methods and the lack of a fully rigorous mathematical basis, the best approach is to use as many extrapolation techniques as possible. This approach helps comparing the results obtained with different approaches providing consistency and a validation element. The results are summarized in Table 8, illustrating reliable results.

		EUR			
Method	Plot	Well A01	Well A06	Well A28	
	$log(q_o)$ vs. t	52.40MM	33.37MM	12.45MM	
DCA	q_o vs. N_p	52.36MM	63.32MM	12.40MM	
	$1/q_o$ vs. t_o	52.36MM	64.10MM	12.50MM	
	$log(f_w)$ vs. N_p	52.67MM	64.32MM	12.40MM	
Semi-steady State WOR	f_o vs. N_p	52.51MM	63.52MM	12.80MM	
	$1/f_w$ vs. N_p	52.67MM	64.80MM	12.80MM	
X-function	X-plot	52.40MM	64.00MM	12.30MM	

Table 8. EUR Results

4. Declarations

4.1. Author Contributions

Conceptualization, S.K.E. and W.M.M.; methodology, W.M.M.; formal analysis, S.K.E. and W.M.M.; writing—original draft preparation, S.K.E. and W.M.M.; writing—review and editing, S.K.E. and W.M.M. All authors have read and agreed to the published version of the manuscript.

4.2. Data Availability Statement

Data sharing is not applicable due to a specific agreement with the company that provided the data.

4.3. Funding

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4.4. Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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